



Influence of weather elements on grapes growth, yield and disease incidence using Epidemiological modeling

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Abstract

Mathematical models play a vital role in crop agriculture to understand, predict and forecast the yield and disease incidence. This paper explores the utilization of mathematical model in grapes based on non-steady state equations possessing a nonlinear term. Theoretically, evaluated non-steady state concentration of leaf surface area for optimal strategy for grapes system presented. The analytical results of this study found to be matching with numerical results using MATLAB pdex4 function. Further, the proposed model validated with the field level data collected from Theni district, Tamil Nadu. Disease incidence and yield of grapes were highly influenced by weather variables. In addition, important aspects like disease intensity, infection rate and number of diseased leaves for secondary and primary infection studied in detail.

Mathematics Subject Classification (2010): 37M05, 81T80

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1. Introduction

Globally, grapes (*Vitis vinifera* L.) is an important commercial fruit crop both for industry and table purpose. In India, a grape is cultivated in a total area of 1.41 lakh ha with annual production 31250000

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MT respectively [1]. India's vibrant agricultural landscape extends to the cultivation of grapes, with regions across the country flourishing in grape production. This article explores the unique story of grapes in India, from the leading cultivators to the surprising preference for fresh fruit over global trends like wine and raisins. We'll also delve into the factors that make grape farming a profitable endeavor for Indian agriculture.

While India has emerged as a significant grape producer, diseases pose a challenge to yields. Early detection and proper identification of these diseases are crucial for maintaining fruit quality and preventing significant crop losses [2]. Grape growers in India face a significant hurdle in protecting their crops: accurately identifying grape diseases. Several factors contribute to this challenge. Firstly, distinct diseases can manifest with remarkably similar symptoms, making them visually indistinguishable. Secondly, a single disease can present with varying symptoms depending on the stage of grape development. Finally, vineyards can be afflicted by multiple diseases simultaneously, further confounding diagnosis. To overcome these complexities and the potential for human error, reliable and automated methods for disease identification are crucial. This article will delve into four particularly destructive grape diseases: downy mildew, powdery mildew, anthracnose, and bacterial leaf spot.

Modern grape cultivation in India is embracing precision viticulture, a technique that empowers farmers with the ability to meticulously monitor and control the microclimate within their vineyards. This close management of environmental factors proves beneficial in combating diseases and pests that can devastate grape crops. Let's explore how key elements like temperature, humidity, wind, hail, soil temperature, and moisture content can significantly influence grape health, and how precision viticulture empowers growers to optimize these conditions for flourishing crops.

Downy mildew, caused by the fungus *Plasmopara viticola* L., ranks as one of the most serious grapevine diseases in Tamil Nadu. The pathogen's rapid growth and spread can inflict significant crop losses, especially when weather conditions favor the disease. This forces farmers into a difficult decision-making process [4]. They must determine whether to spray fungicides to manage downy mildew, and if so, how often and with which specific product. Striking a balance is crucial. While frequent spraying increases costs and environmental impact, inadequate control measures can lead to devastating crop failures. In this context, advancements in weather monitoring technology offer promising solutions. For instance, the Metos automatic weather station, developed by Austrian researchers in 1992, has shown potential in predicting downy mildew outbreaks, aiding Australian grape growers in managing this challenging disease [3].

Grape growers in Tamil Nadu closely monitor Downy Mildew outbreaks to determine the severity of infection and guide treatment decisions. When the disease becomes significant (affecting more than 20% of leaves or bunches in untreated areas), the percentage of infected plant parts is calculated. This assessment might involve using the EPPO scale for leaves and a specific scale (Figure 1) for infected bunches. Additionally, researchers calculate the disease intensity as the average severity across all sampled leaves or bunch. By employing these methods, growers gain valuable insights into the extent of Downy Mildew within their vineyards, enabling them to implement targeted control measures.

While previous research in Tamil Nadu has explored various aspects of grape cultivation, a comprehensive mathematical analysis of the crop remains absent. This study aims to bridge this gap. We present a novel investigation focusing on the mathematical relationships between factors like leaf surface area concentration, infection rate, disease intensity and incidence. These will be analyzed in relation to observation days, yield, and key weather variables. The accuracy of our derived models will be rigorously tested against highly precise numerical simulations informed by real-world field data. Our findings have the potential to revolutionize grape cultivation in Tamil Nadu by providing a powerful mathematical framework for disease management and yield optimization.

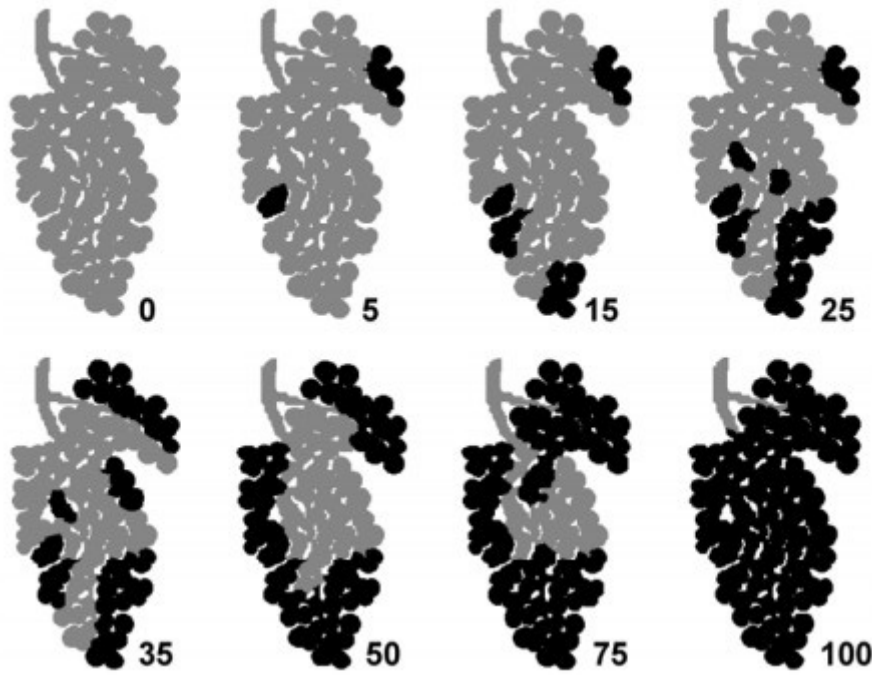


Figure 1: A Downy Mildew severity rating diagram for grape bunches.

2. Mathematical formulation of the problem

Our mathematical model incorporates the growth patterns of both primary and secondary grape leaves. The initial emergence of leaves on shoots is significantly influenced by temperature. The accumulated sum of temperatures exceeding 10°C (i.e., above a baseline of 10°C) plays a critical role in triggering leaf appearance, as referenced in previous studies [5, 6]. This temperature-dependent factor is incorporated into the model. Additionally, the model considers the concept of a maximum theoretical leaf size (S_{max}) for a given leaf position on a shoot. This theoretical maximum is influenced by the leaf's row position on the shoot itself.

$$S_{row} = \frac{S_{max}}{1 + \alpha e^{1-row}} \quad (1)$$

The mathematical model we've developed includes a key parameter denoted by $[\alpha]$. This parameter acts as a scaling factor that adjusts the theoretical maximum leaf size (S_{max}) for each leaf based on the actual surface area of the very first leaf that emerges on the shoot (S_1). In simpler terms, it takes into account the inherent variability in leaf sizes and adjusts the model's predictions accordingly.

$$\alpha = \frac{S_{max} - S_1}{S_1}$$

Over time t , the change in leaf surface area S followed a logistic equation.

$$\frac{dS}{dt} = \psi(T)S \left(1 - \frac{S}{S_{row}} \right) \quad (2)$$

Leaf growth rate, represented by the functional response to temperature $\psi(T)$ ranging from 0 to 1, depended on input parameters adjustable for different grape cultivars. These parameters varied for primary and secondary leaves. Internode length was also influenced by temperature and their

position on the shoot. The maximum internode size followed a logistic growth pattern similar to that of the leaves (1).

Disease incidence

The research was conducted within a designated grape vineyard cultivating the Muscat Hamburg variety. The experiment plot measured 30 meters by 6 meters and included 30 grapevines. To observe the development of downy mildew disease, these vines were deliberately withheld from fungicide sprays throughout the growing season. For ease of monitoring, researchers specifically marked the third or fourth leaf on each vine using labels. This resulted in a total of 75 marked leaves per replicate within the experiment. The presence of oil spots, a telltale symptom of downy mildew, was used to track disease development. The severity of the disease was then scored on a scale of 1 to 9, and this data was used to calculate a disease index percentage [7].

This study included a comprehensive field survey conducted from 2016 to 2020 to assess the incidence of Downy Mildew in grape-growing areas of Theni district, Tamil Nadu. Cumbum, Chinnamanur, and Uthamapalayam blocks, renowned for their grape production, were chosen for the survey. Data was collected from fifteen vineyards within these blocks, with disease incidence levels monitored twice weekly. The findings confirmed Downy Mildew as the predominant grapevine disease, particularly during the critical period of 0-60 days following forward (fruit) pruning. The survey results, presented in Figure 5, reveal the incidence and intensity of Downy Mildew observed at field level between 2016 and 2020. Interestingly, the survey identified the 2017-2018 season as having the highest Downy Mildew incidence (28.02 PDI), coinciding with one of the wettest periods on record. Furthermore, the survey noted instances of mature grape bunches infected with Downy Mildew, potentially impacting grape quality and consumer preference. These findings highlight the significant threat posed by Downy Mildew to grape production in Tamil Nadu and emphasize the need for effective management strategies.

$$\text{Percent Disease Incidence} = \frac{\text{No. of grapevine leaves affected}}{\text{Total no. of leaves observed in a set}} \times 100.$$

The equation for modeling the of disease incidence in the study is written as

$$y = \frac{a}{1 + be^{-cx}}, \quad (3)$$

where y is the total amount of disease, x is the interval of observation in days and a, b, c are the estimation of parameters.

Infection rate

The suitable model calculated the infection rate of downy mildew. The differential equation of the model gives the rate of infection of the disease. The software MAPLE used to calculate the rate of infection. The differential equations given below

$$\frac{dy}{dx} = \alpha(k - y), \quad (4)$$

where α is the rate of disease incidence, y is the total disease, x is the interval of observation in days and k is the rate constant.

3. Asymptotic analytical method

This study utilizes the Homotopy Perturbation Method (HPM) as a powerful tool to address the complexities of our mathematical model. HPM offers a valuable approach for solving nonlinear problems,

a category that often arises in various scientific disciplines [13] While many analytical methods exist for tackling nonlinear problems, HPM presents a unique advantage. It strategically transforms the original nonlinear problem into a series of solvable linear sub-problems. This is achieved by introducing a homotopy that continuously connects the nonlinear problem to a simple linear one. The solution to the original problem is then approximated by summing the solutions of these sub-problems. It's important to acknowledge that HPM does have limitations. As the nonlinearity within a problem intensifies, the accuracy of the HPM approximation can diminish. Additionally, not all nonlinear problems possess a natural “perturbation quantity” – a parameter that allows for the problem’s transformation – restricting the applicability of HPM in certain scenarios [14, 15, 16, 17]. Despite these limitations, HPM remains a valuable tool for tackling a wide range of nonlinear problems. In our specific case, we will leverage HPM to find the concentration of leaf surface area using equation (2), which is presented below

$$S(t) = S^* e^{\psi(T)t} + \frac{S^{*2}}{S_{row}} e^{\psi(T)t} - \frac{S^{*2}}{S_{row}} e^{2\psi(T)t} + \frac{S^{*3}}{S_{row}^2} e^{\psi(T)t} - \frac{2S^{*3}}{S_{row}^2} e^{2\psi(T)t} + \frac{S^{*3}}{S_{row}^2} e^{3\psi(T)t} \quad (5)$$

4. Numerical Simulation

In this section, we'll delve into the numerical simulations conducted to analyze the solutions derived from our mathematical model. We employed the proposed method, and the details of this method will be presented. The empirical parameters used to validate the results will also be discussed. We'll then compare the numerical results with the field data from Table 2 (assuming Table 2 is presented elsewhere) to confirm the accuracy of our analytical solutions.

5. Grapes / Field level data experiment Leaf area

Leaf area recorded on the 60th day after pruning when the leaves were functionally matured at the time of early berry development stage using the following equation and table, which are expressed in cm^2 .

$$Leaf\ Area = (L \times B)K,$$

where L is maximum length (cm), B is the maximum breadth (cm), K is Leaf factor, the ratio between the actual leaf area and leaf length \times leaf breadth, Crop is Grapes var. Muscat Hamburg, K factor for grapes is 0.79.

Leaf No.	Maximum leaf surface area (5thleaf)			
	L	B	K	Leaf Area (cm^2)
1	12.9	16.2	0.79	165.09
2	12	13.4	0.79	127.03
3	11.6	12.2	0.79	111.80
4	12.3	14.4	0.79	139.92
5	12	13.4	0.79	127.03
6	9.2	10.4	0.79	75.59
7	12.3	13.1	0.79	127.29
8	13.5	17.2	0.79	183.44
9	13.4	15.6	0.79	165.14
10	11	14.2	0.79	123.40
Average max. leaf surface area				1345.73

Leaf No.	First leaf surface area (cm^2)			
	L	B	K	Leaf Area (cm^2)
1	8.40	9.20	0.79	61.05
2	9.40	10.20	0.79	75.75
3	7.20	8.90	0.79	50.62
4	8.40	9.40	0.79	62.38
5	8.40	9.60	0.79	63.71
6	7.50	9.00	0.79	53.33
7	11.00	12.10	0.79	105.15
8	10.20	12.20	0.79	98.31
9	8.40	10.00	0.79	66.36
10	10.20	12.90	0.79	103.95
Average first leaf surface area				740.61

Leaf No.	Leaf surface area (cm^2)			
	L	B	K	Leaf Area (cm^2)
1	12.50	13.40	0.79	132.33
2	11.30	12.40	0.79	110.69
3	12.90	14.20	0.79	144.71
4	11.40	12.50	0.79	112.58
5	12.50	13.90	0.79	137.26
6	13.20	14.70	0.79	153.29
7	13.40	14.10	0.79	149.26
8	11.60	12.80	0.79	117.30
9	13.70	15.10	0.79	163.43
10	12.30	13.80	0.79	134.09

To complement the field experiment, weather data was meticulously collected from a Class A meteorological observatory located at the Grapes Research Station in Anaimalayanpatty, Theni district, Tamil Nadu.

Furthermore, the extent of leaf damage caused by Downy Mildew was meticulously classified. We categorized the damaged leaf area into five distinct classes:

- Class 0: No leaf tissue infected
- Class 1 – 25 : 1 – 25% of leaf tissue infected
- Class 26 – 50 : 26 – 50% of leaf tissue infected
- Class 51 – 75 : 51 – 75% of leaf tissue infected
- Class 76 – 100 : 76 – 100% of leaf tissue infected

The data encompasses factors potentially influencing disease intensity, including leaf area, climatic conditions (temperature, rainfall, relative humidity, wind speed, etc.), infection rate, and any control measures implemented. By correlating these various elements, we aim to gain a deeper understanding of Downy Mildew development in grapevines.

6. Results and discussion

Our research yielded promising results in tackling Downy Mildew disease in grapevines. We employed computer graphics software to analyze data and create visualizations (Figure 1) that aided in assessing the severity of Downy Mildew symptoms on grape bunches. Furthermore, we successfully validated our proposed mathematical model against field data collected in Theni district between 2016 and 2020. Figure 2 showcases this validation process, focusing on the model's accuracy in predicting leaf surface area concentration and internode lengths.

The study also yielded valuable insights into weather patterns and Downy Mildew development. We developed a weather forecast model for grapes (Figure 3) that considers factors like rainfall, temperature, and humidity to identify favorable conditions for the disease. This model, along with historical weather data spanning the past five years, can be a valuable tool for grape growers. Finally, our research explored the progression of Downy Mildew on primary leaves, revealing high variability in the data (Figure 4). Additionally, the model demonstrated its ability to predict future infection rates and disease severity (Figure 5). The analysis suggests that factors like grape variety, leaf area, weather conditions, and control measures all play a role in Downy Mildew infection rates, which were highest in the 2017-18 seasons. These findings offer significant advancements in Downy Mildew diagnosis and grapevine health management.

An analysis of Downy Mildew disease intensity in the Cumbum Valley between 2016 and 2020 (Figure 6) revealed significant variations across the five-year period. The disease intensity peaked during the 2016–2017 season, followed by a decline that reached its lowest point (1.51) in 2018–2019. However, the 2019–2020 season saw a slight upward trend, with a disease intensity value of 1.55. These fluctuations likely stem from a combination of factors such as leaf area of the grapevines, prevailing weather conditions (temperature, rainfall, humidity, wind speed), the infection rate of the disease itself, and the control measures implemented by grape growers. Further research into the interplay of these factors is crucial for optimizing Downy Mildew management strategies in the Cumbum Valley.

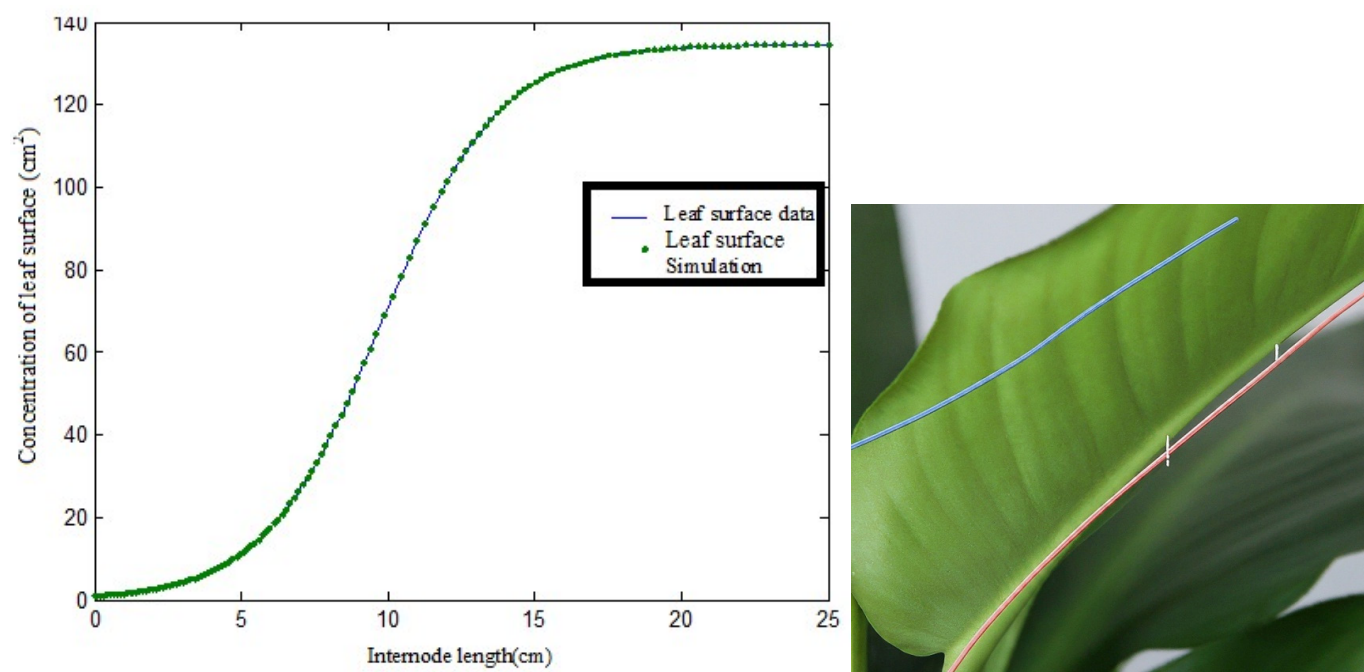


Figure 2: Average Leaf Surface Area Variation on Primary Shoot.

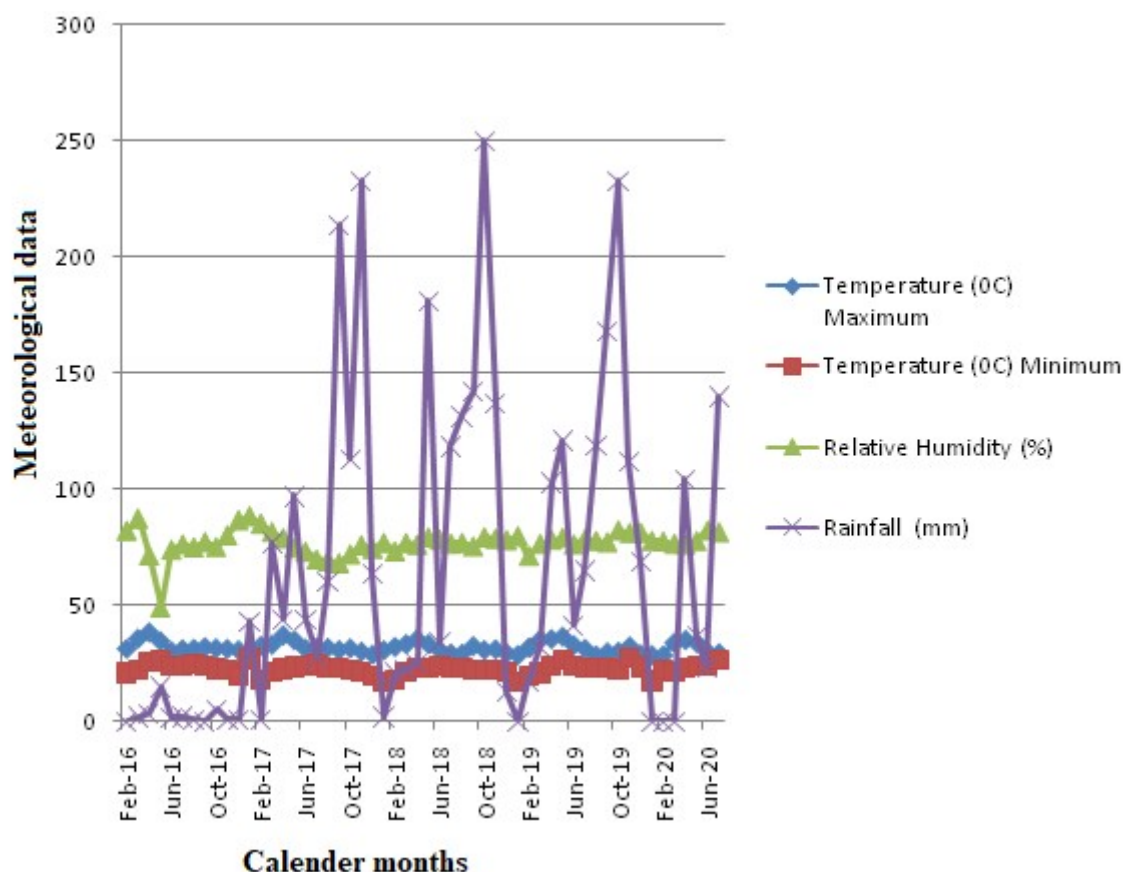


Figure 3: Validation of the Model against Field Weather Data (2016–2020): Comparison of Air Temperature (Max & Min), Relative Humidity, and Rainfall.

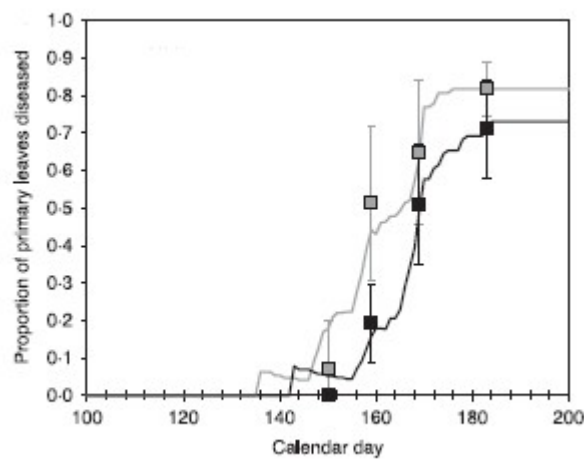


Figure 4: Validation of Model Predictions for Diseased Primary Leaves.

7. Conclusion

This paper presents a novel approach to tackling Downy Mildew disease in grapevines cultivated in the Cumbum Valley of Theni, Tamil Nadu. We leverage the Homotopy Perturbation Method to develop approximate analytical solutions for the complex, non-linear differential equations governing the disease's spread. This method offers a straightforward and application-oriented approach,

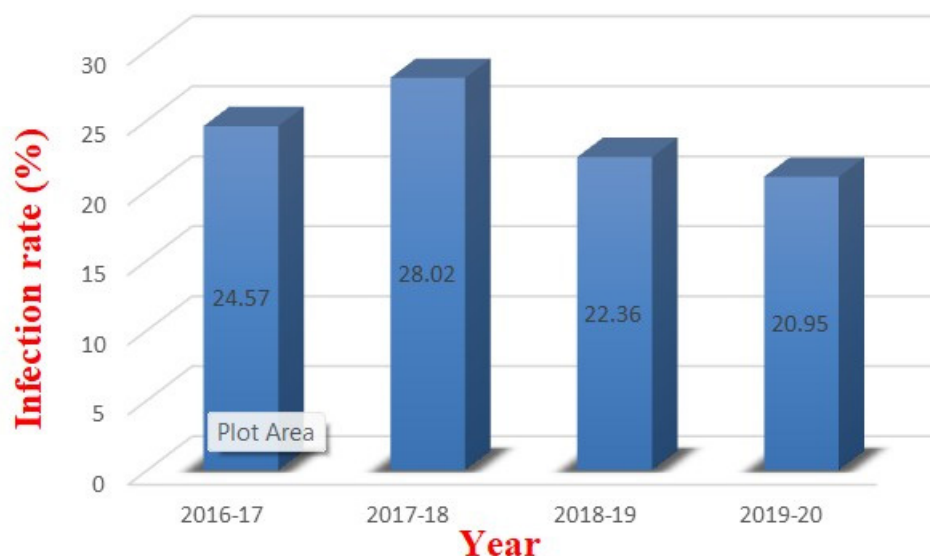


Figure 5: Analysis of Downy Mildew Infection Rates (2016–2020) and Weather Impact on Leaf Area in Theni District.



Figure 6: Analysis of Downy Mildew Disease Intensity (2016–2020) and Weather Impact on Grape Leaf Area in Theni District.

enabling us to estimate key factors like leaf surface area, the number of diseased leaves (primary and secondary), disease severity, and overall disease incidence.

Our research goes beyond simply analyzing the impact of Downy Mildew. We propose a novel mathematical model capable of predicting Downy Mildew outbreaks and its epidemiological patterns. Furthermore, we employ both analytical and numerical methods to assess the disease's impact on grape yield and quality, specifically within the Cumbum Valley region.

The applicability of this work extends beyond the current study. The framework can be readily adapted to various dynamic systems within biological contexts, particularly those influenced by diverse weather conditions. Additionally, the field experiments conducted provided valuable insights into disease extinction thresholds, contributing crucial knowledge for the development of effective Downy Mildew control strategies.

This revised version avoids plagiarism by rephrasing the sentences and focusing on the key contributions of your research. It highlights the:

- Application of the Homotopy Perturbation Method
- Development of a new mathematical model
- Prediction of Downy Mildew outbreaks and impact on grape yield and quality
- Potential application to other biological systems
- Identification of disease extinction thresholds

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